

Name: Answer Key

**UNIT #3 Study Guide
COMMON CORE ALGEBRA I**

Study Guide

PART I QUESTIONS: Answer all questions in this part. Show all of your work.

1. If $g(x) = 5x + 2$ and $f(x) = x^2 - 4$ then which of the following is the value of $g(-6)$ and $f(-5)$?

$$\begin{aligned} g(-6) &= 5(-6) + 2 \\ g(-6) &= -30 + 2 \\ \boxed{g(-6)} &= -28 \end{aligned}$$

$$\begin{aligned} f(-5) &= (-5)^2 - 4 \\ f(-5) &= 25 - 4 \\ \boxed{f(-5)} &= 21 \end{aligned}$$

OR USE
the calculator
Enter what is after
the equal sign.

Substitute
into
 g

Substitute
into
 f

2. If a function is defined by the formula $f(x) = \frac{1}{4}x - 2$ and its domain is given by the set $\{-8, -4, 0, 4\}$

which of the following sets gives the function's range?

• Substitute •

x	y
-8	-4
-4	-3
0	-2
4	-1

{ $\underline{-4}, \underline{-3}, \underline{-2}, \underline{-1}$ }
range

$$\begin{aligned} y &= \frac{1}{4}(-8) - 2 & y &= \frac{1}{4}(-4) - 2 & y &= \frac{1}{4}(0) - 2 \\ y &= -2 - 2 & y &= -1 - 2 & y &= 0 - 2 \\ y &= -4 & y &= -3 & y &= -2 \\ \boxed{y = -4} & & \boxed{y = -3} & & \boxed{y = -2} & \\ & & & & & \boxed{y = -1} \end{aligned}$$

all of these points are on the line.

3. The distance, d , that a car has traveled, as a function of time, t , is given in the table below. What is the average rate of change of the distance over the interval $4 \leq t \leq 10$ ← use these numbers

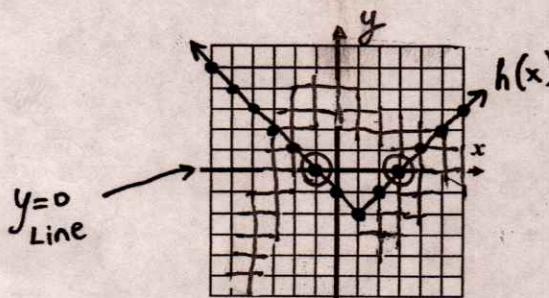
d (miles)	0	119	150	271	332	468
t (hours)	0	2	4	6	8	10

• determine the distance and the number of hours during the given interval.

$$\begin{array}{c} d \quad t \\ \hline 4 \quad 150 \\ 10 \quad 468 \\ \hline +6 \quad +318 \\ \text{hours} \quad \text{Miles} \end{array}$$

$$\frac{468 - 150}{10 - 4} \text{ miles per hour} = \frac{318}{6} = 53 \text{ mph}$$

4. For the function $h(x)$ shown graphed below, over which of the following intervals is



$y \leq 0$
Less than or equal to

$$-1 \leq x \leq 3$$

The part of the graph below the x-axis.

$$(-1, 0) \quad (3, 0)$$

5. For the function defined by $f(x) = \begin{cases} 3x-1 & x < 5 \\ 3x-1 & x \geq 5 \end{cases}$, which of the following represents the value of $f(6)$? less than

$$f(6) = 3(6) - 1$$

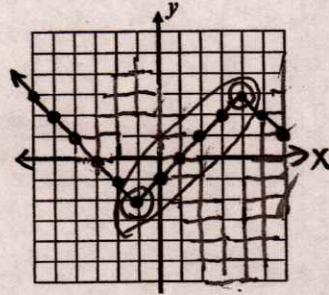
$$f(6) = 18 - 1$$

$$f(6) = 17$$

↑ or use the calculator Should you substitute into the top or bottom? why? bottom because $6 \geq 5$. ↑ greater than or equal to

6. For function $g(x)$ graphed below, over which of the following intervals is $g(x)$ increasing?

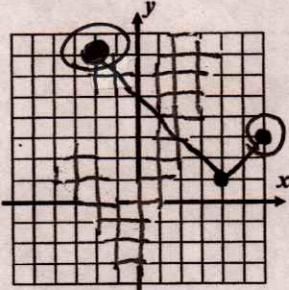
$$\frac{-1}{(-1, -2)} \leq x \leq \frac{4}{(4, 3)}$$



↑ from left to right the graph should go up

7. Given the graph of the function $f(x)$ shown below, which of the following intervals represents its domain?

$$\frac{-2}{\text{far left}} \leq x \leq \frac{6}{\text{far right}}$$



Define domain: It explains how wide the function is on a graph.

What is the difference between an open circle and a closed circle? excluded, included in the domain

8. A function is initially defined by the set of coordinate pairs $\{(-2, 6), (-5, 4), (7, -3)\}$. Which coordinate pair below, if added to this set, prevents the set from representing a function?

$$\left(\underline{-2}, \underline{\text{any}} \right) \text{ or } \left(\underline{-5}, \underline{\text{any}} \right)$$

$$\left(\underline{7}, \underline{\text{any}} \right)$$

Explain why? I made the x values repeat. So, it is not a function.

Define a non-function; it has repeating \underline{x} values.

9. If the function $h(x)$ is defined by $h(x) = 3x$ then which of the following values of x solves the equation $h(-12)$?

$$h(-12) = 3(-12)$$

$$h(-12) = -36$$

x	$h(x)$
-12	-36

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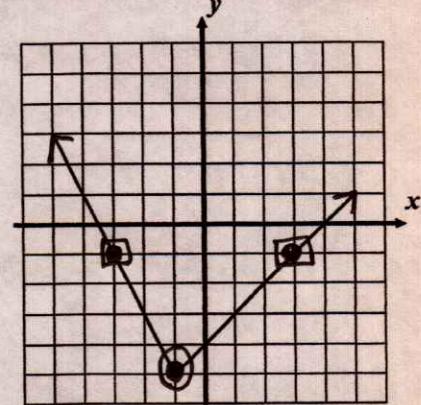
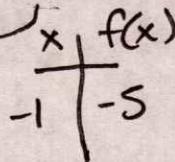
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PART II QUESTIONS: Answer all questions in this part. Show all of your work.

Algebra

10. The function $f(x)$ is shown on the graph. What point does $f(-1)$ represent? Circle this point on the graph.

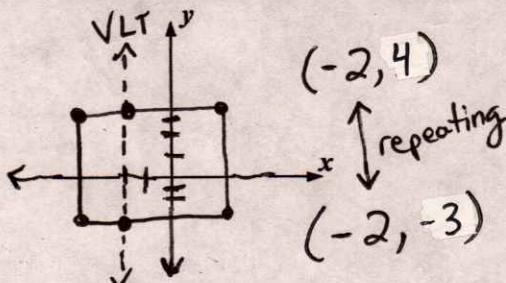
$$(-1, -5)$$



11. What point(s) does the value of $f(x) = -1$ represent? Box the point(s).

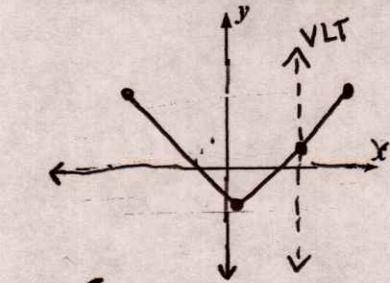
$$(-3, -1) \text{ and } (3, -1)$$

- 12-13. Do the following graphs represent functions? Explain how you arrived at your choice.



draw a non-function

Explain: repeating x values



draw a function

Explain: VLT has only one point.
x values do not repeat.

- PART III QUESTIONS: Answer all questions in this part. Show all of your work.

14. Two functions, $f(x)$ and $g(x)$, are given below. Determine which of these functions has the greater average rate of change over the interval $1 \leq x \leq 5$.

The average rate of change shows ...

x	1	5
<u>$g(x)$</u>	2	34

x	0	1	2	3	4	5	6
$g(x)$	0	2	4	8	16	34	68

$$\begin{array}{c} x | g(x) \\ \hline 1 | 2 \\ 5 | 34 \end{array}$$

4 < $\frac{32}{5}$ > 32

Average Rate of Change for $g(x)$

Average Rate of Change for $g(x)$

Algebra

Unit 3

15. Graph the piecewise function shown below on the axes provided. Which point below is on the graph?

$$f(x) = \begin{cases} -3x - 8 & -4 \leq x < -1 \\ 2x - 3 & -1 \leq x \leq 3 \end{cases}$$

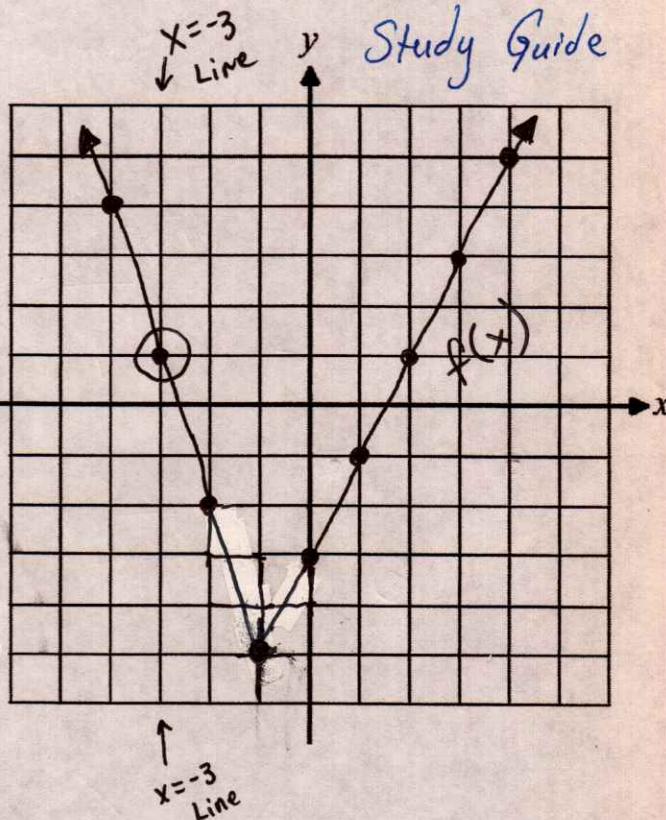
x	f(x)
-4	4
-3	1
-2	-2
-1	-5

x	f(x)
0	-3
1	-1
2	1

16. What is the value of $f(-3)$ for this piecewise function?
Circle this point on your graph.

which point is $f(-3)$?

$$\left(\frac{-3}{x}, \frac{1}{y} \right) \quad -3 \neq 1$$



PART IV QUESTION: Answer the question in this part. Show all of your work.

17. For the function $f(x)$ shown graphed below answer the following questions.

State the domain and range $(-4, -5) \rightarrow (-4, 5)$

$\frac{-4}{\text{how far left?}} \leq x \leq \frac{7}{\text{how far right?}}$

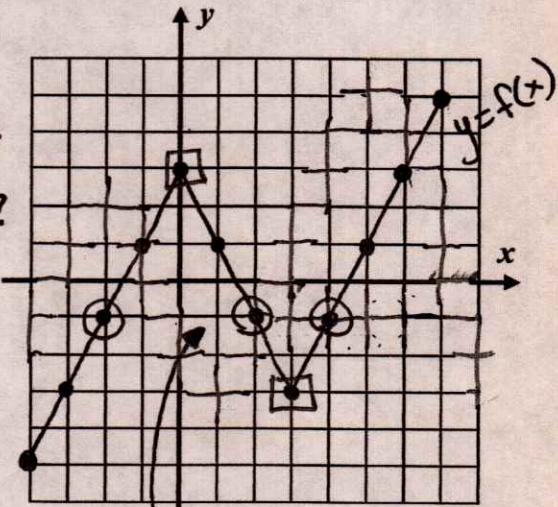
$\frac{-5}{\text{how low?}} \leq f(x) \leq \frac{5}{\text{how high?}}$

18. What values of x solve the equation $f(x) = -1$

Circle points on your graph that justify your solution.

There are 3 x-values on $f(x) = -1$

$$x = \left\{ \frac{-2}{\text{Left}}, \frac{2}{\text{Top of the hill}}, \frac{4}{\text{Right}} \right\}$$



19. Give the intervals over which $f(x)$ is decreasing, and, circle the decreasing sections on the graph.

$$\frac{0}{\text{Look at the graph}} \leq x \leq \frac{3}{\text{Top of the hill}}$$

Left

(Bottom of the hill)

$$(0, 3)$$

$$\frac{3}{\text{Right}} \leq x \leq \frac{-3}{\text{Bottom of the hill}}$$

Right

(Bottom of the hill)

$$(3, -3)$$

decreasing interval

from Left to right it is going down.